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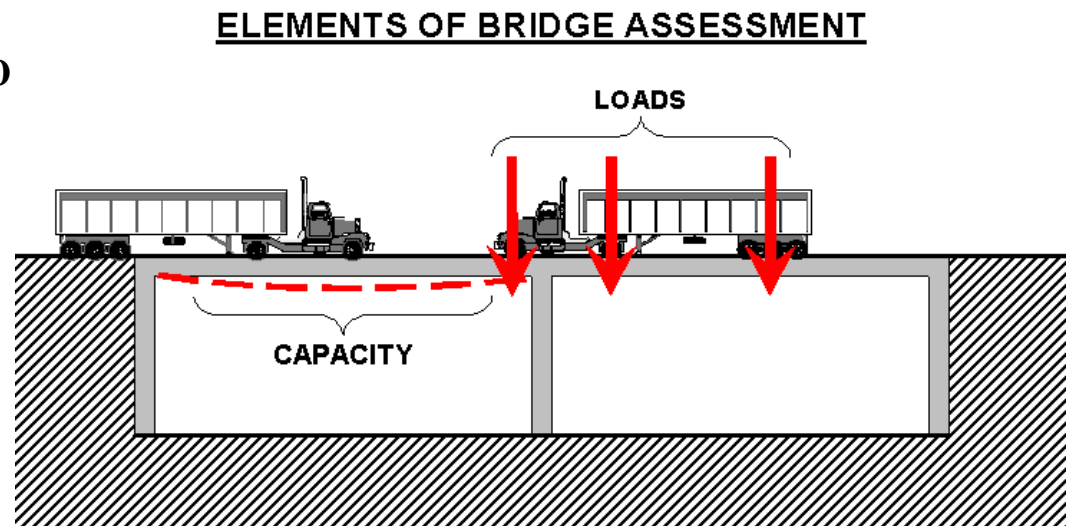
**Finding the Distribution of Bridge Lifetime Load Effect
by Predictive Likelihood**

Finding The Distribution of Bridge Lifetime Load Effect by Predictive Likelihood

C.C. Caprani & E.J. OBrien

Introduction

- About **€6 bn** is spent in the **EU annually** on bridge repair and replacement
- Thus it is **costly** and also very **disruptive**
- Short- to medium-length (20-50 m) bridges are the most common
- The assessment of **bridge capacity** is relatively accurate
- **Load assessment** is difficult & less accurate due to large variations in traffic



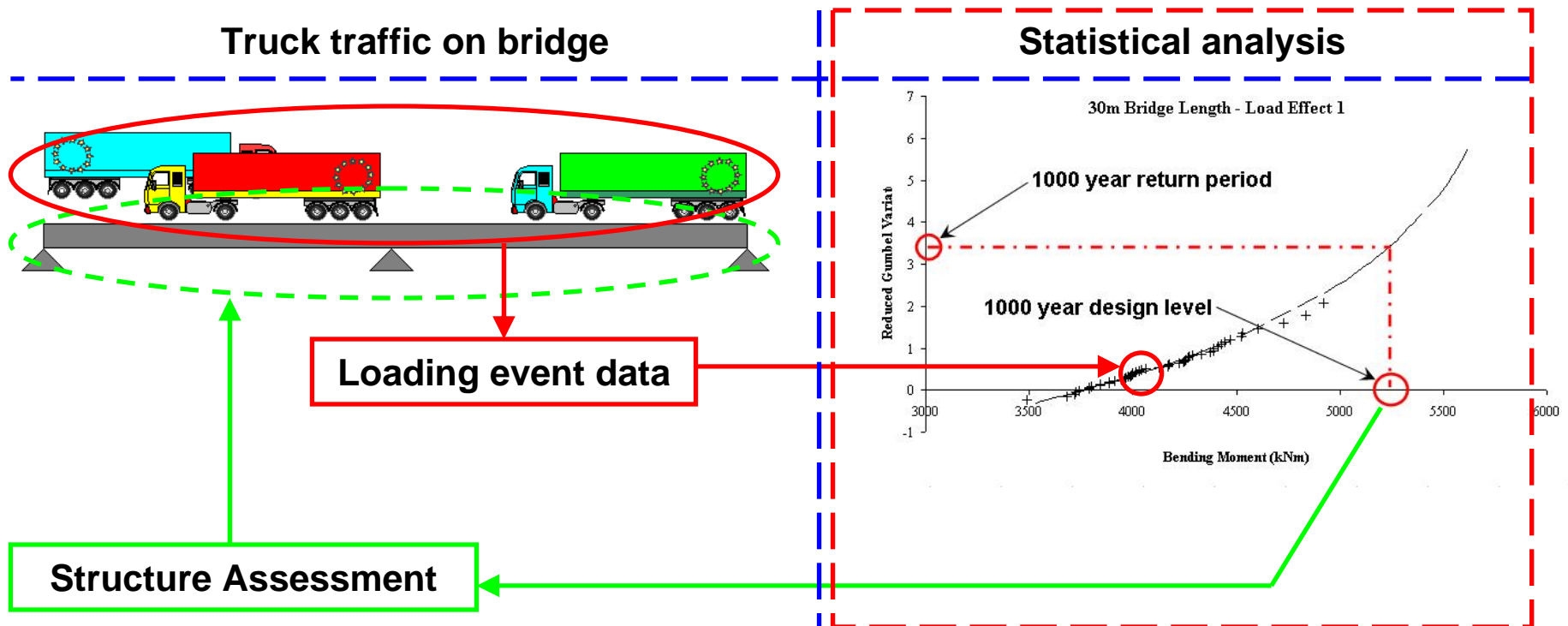
Conclusion: There are large **potential savings** through accurate **load assessment**

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Assessment Process

— Represents this work's area of interest

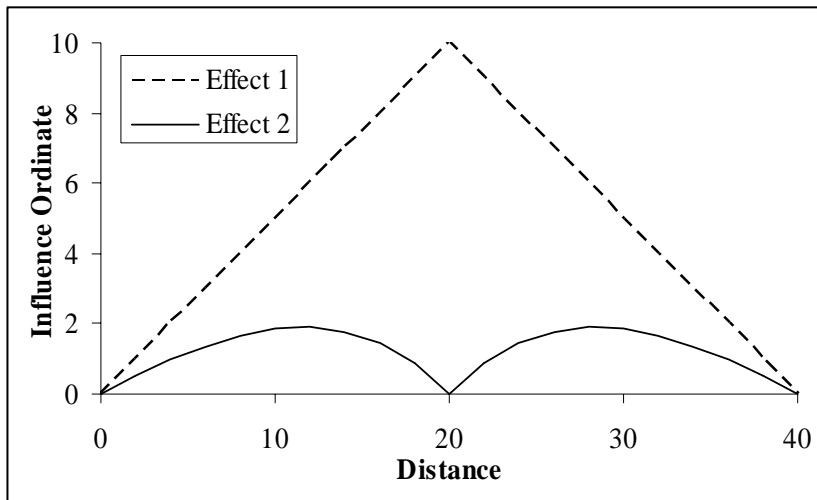


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Traffic Load Simulation

- Real traffic is measured using **Weigh-In-Motion** technology
- The traffic's **characteristics** are statistically modelled
- **Monte Carlo simulation** from these models allows much more traffic to be studied



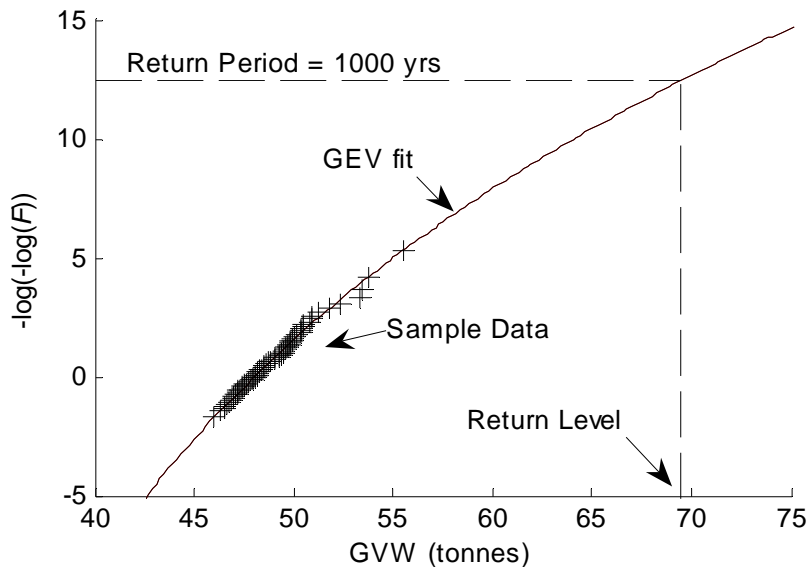
- Generated traffic is passed over the **influence lines** of interest to obtain the bridge traffic load effect

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Standard Statistical Analysis

- **Extreme value analysis** is usually used (block maxima or POT)
- Using block maxima, for the load effect/characteristic of interest:



1. **Daily maximum** values (typically) are noted (stationarity)
2. A **GEV distribution** models the data
3. The required **return level** is obtained (1000-years for EC1.3)

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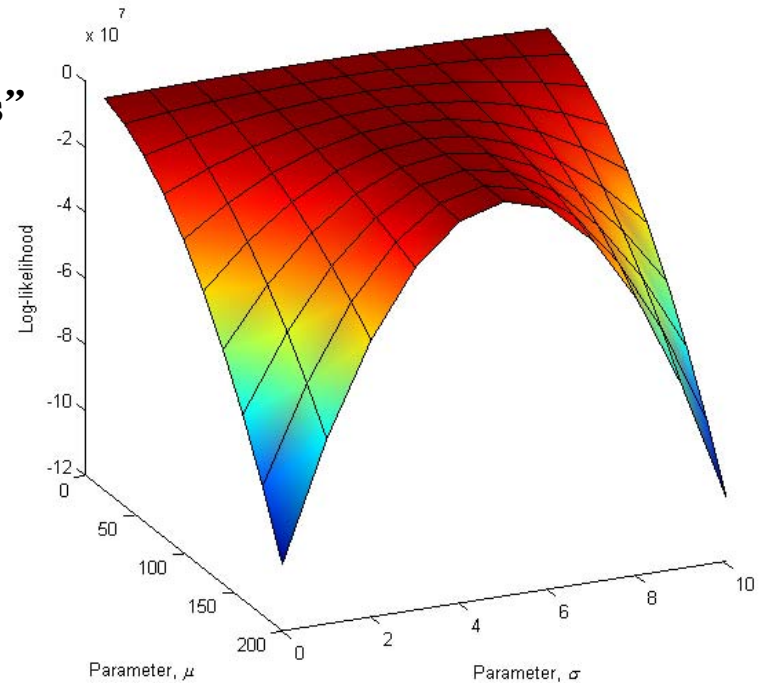
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Problems

The Eurocode 1.3 **design level** is that with:
“a 10% probability of exceedance in 100 years”

Usually taken as a **1000-year return period**

- **No variability** allowed for in the 1000-year RP prediction
- **Model/fit uncertainty** not taken into account:
 - width of likelihood surface
 - predictions from adjacent fits (near parameter vectors)



Conclusion: The model parameter vector confidence intervals should be taken account of in the prediction

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Predictive Likelihood

- Given the data as the **only true known**
- for a **range** of possible 'prediction-values'
- the predictive likelihood function is evaluated for each
- A distribution of PL values results

The **predictive likelihood function**:

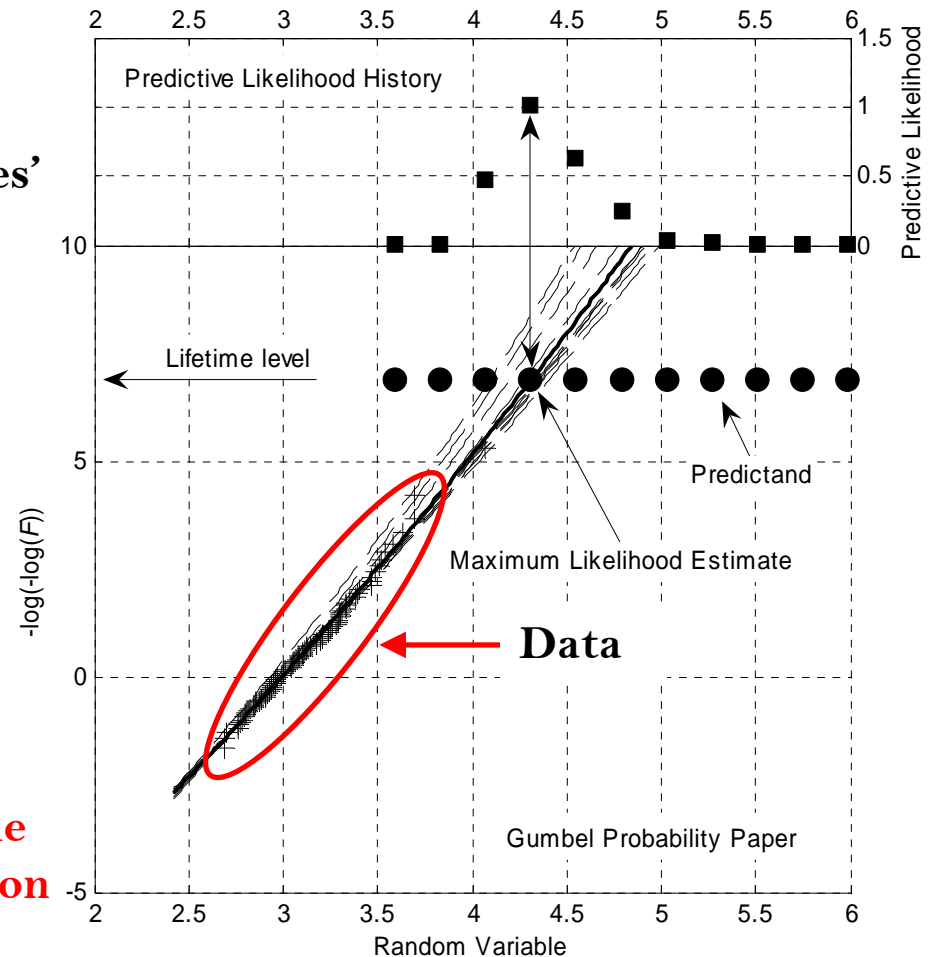
$$L_P(z | y) = \sup_{\theta} L_y(\theta; y) L_z(\theta; z)$$

Best fit of

known
data

&

possible
prediction



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Modifications

The predictive likelihood noted is Fisherian predictive likelihood

Two modifications are made to improve this:

1. **Variability** of the fitted model parameters are included
(the n -dimensional width of the likelihood surface: $\sqrt{|\mathcal{I}(\theta_z)|}$)
2. A vector transformation into the correct **parameter domain** $|\partial\theta_z/\partial\theta|$
(does not affect the shape of the curve due to normalization)

Thus: **Modified Predictive Likelihood:**
$$L_{MP}(z|y) = \frac{L_P(z|y; \theta_z)}{\left| \frac{\partial\theta_z}{\partial\theta} \right| \sqrt{|\mathcal{I}(\theta_z)|}}$$

These changes are **generally insignificant**

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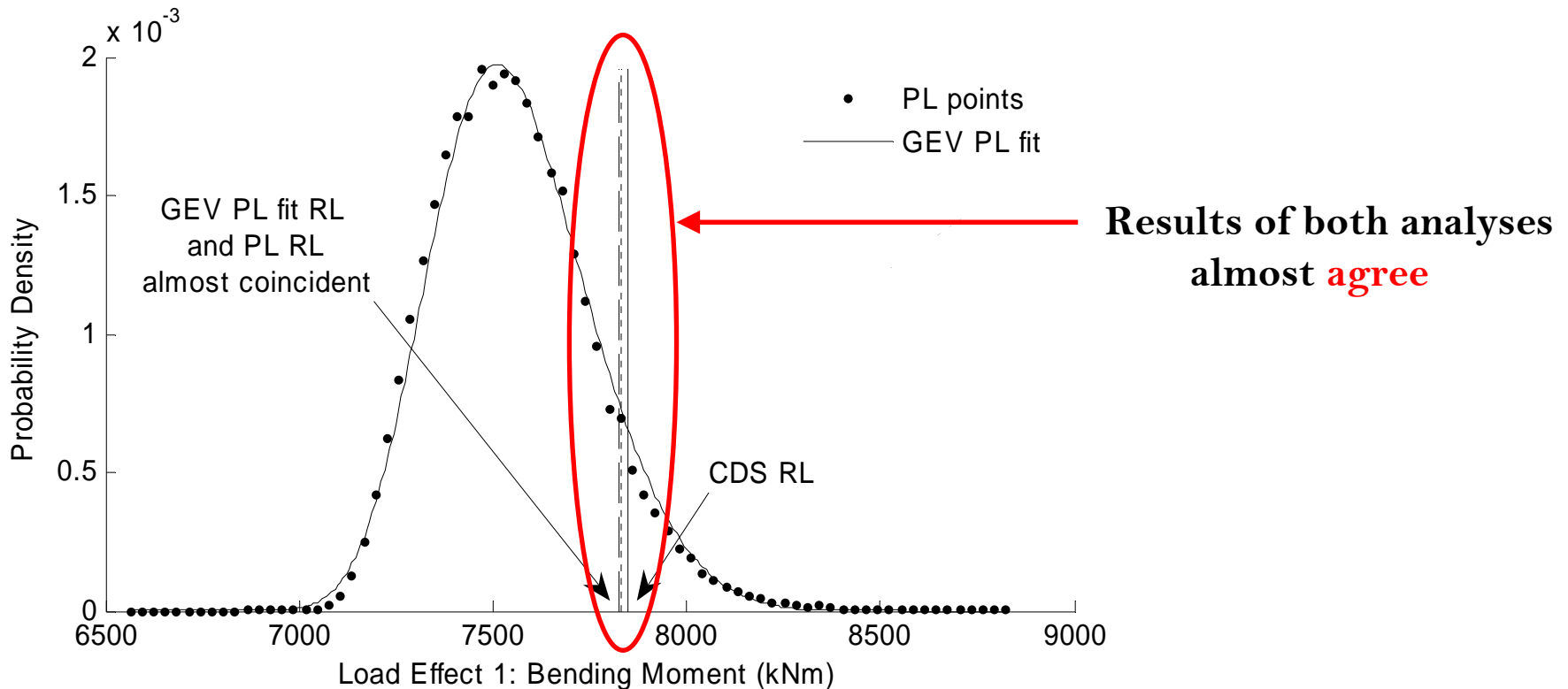
Application

- Data from the A6 **Paris-Lyon motorway** is used
- A 1000-day MC traffic sample is generated
- 1000 **daily maximum** static load effects are noted for:
 1. Load Effect 1: mid-span moment of a simply-supported bridge
 2. Load Effect 2: Left hand shear in a simply-supported bridge
 3. Load Effect 3: Central support moment of a two-span bridge
- **Two forms of analysis** for the design level:
 1. Standard extreme value analysis (1000-year RP)
 2. Predictive likelihood analysis
(the 100-year lifetime load effect distribution)

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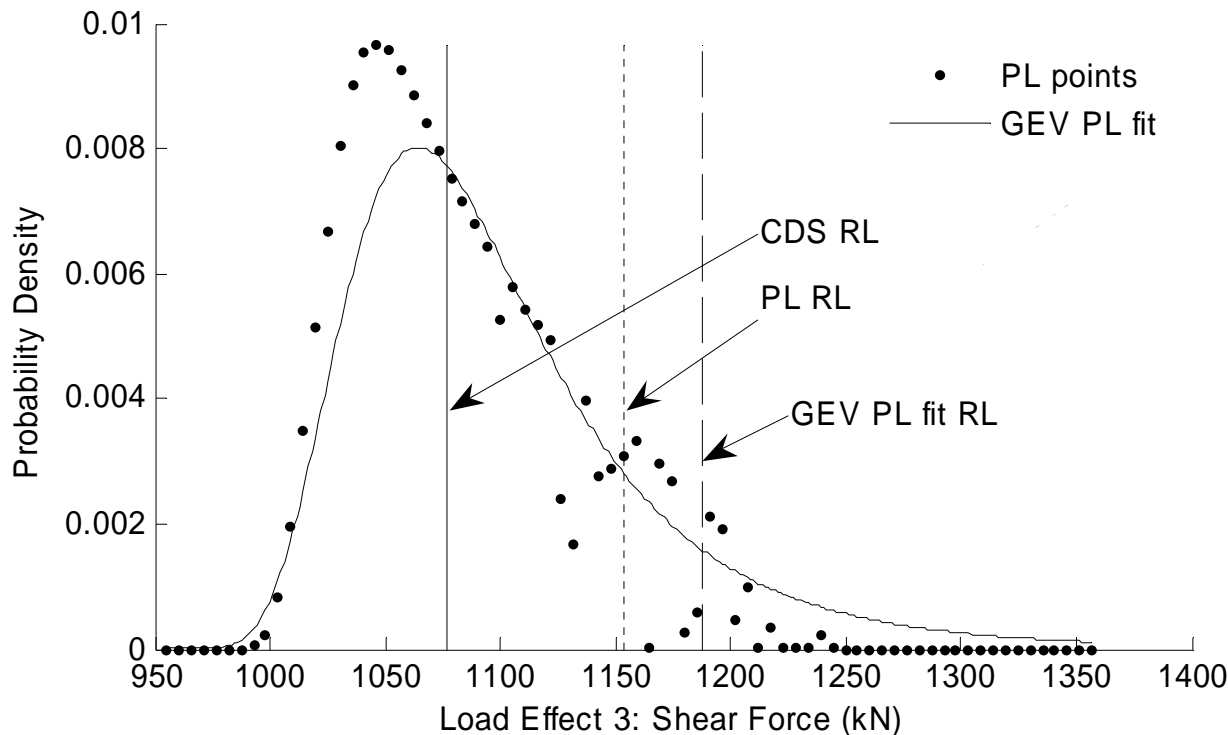
Sample Results - Load Effect 1, 30 m bridge length



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Sample Results - Load Effect 3, 40 m bridge length

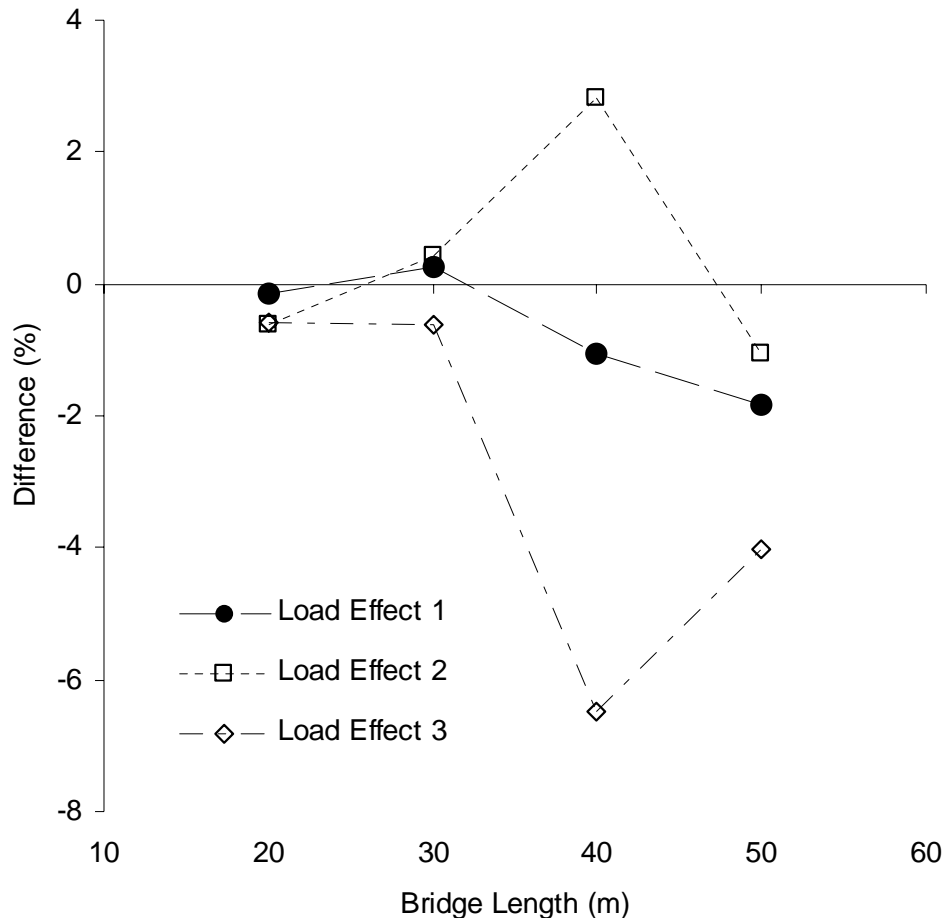


- PL points **less stable** numerically
- 'Best fit' GEV distribution **smoothes** this
- Significantly **different** answer to standard analysis

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General Results



- Percentage difference of standard EV analysis to the PL results
- PL to be preferred as more **information** is returned from sample
- Standard analysis is generally **non-conservative**

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Conclusions

The different results of the

predictive likelihood (100-year with 10% probability of exceedance)

and the

standard EV analysis (1000-year return period)

show these definitions of probability are not equivalent

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Conclusions

Predictive likelihood:

- accounts for more variability
- obtains more information from the sample
- gives the lifetime distribution of load effect
- generally gives slightly more conservative results for the data studied

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